

ASCII Character Conversion

CHAR	HEX	OCTAL	BINARY	DEC	CHAR	HEX	OCTAL	BINARY	DEC
A	41	101	01000001	065	P	50	120	01010000	080
B	42	102	01000010	066	Q	51	121	01010001	081
C	43	103	01000011	067	R	52	122	01010010	082
D	44	104	01000100	068	S	53	123	01010011	083
E	45	105	01000101	069	T	54	124	01010100	084
F	46	106	01000110	070	U	55	125	01010101	085
G	47	107	01000111	071	V	56	126	01010110	086
H	48	110	01001000	072	W	57	127	01010111	087
I	49	111	01001001	073	X	58	130	01011000	088
J	4A	112	01001010	074	Y	59	131	01011001	089
K	4B	113	01001011	075	Z	5A	132	01011010	090
L	4C	114	01001100	076					
M	4D	115	01001101	077					
N	4E	116	01001110	078					
O	4F	117	01001111	079					
a	61	141	01100001	097	p	70	160	01110000	112
b	62	142	01100010	098	q	71	161	01110001	113
c	63	143	01100011	099	r	72	162	01110010	114
d	64	144	01100100	100	s	73	163	01110011	115
e	65	145	01100101	101	t	74	164	01110100	116
f	66	146	01100110	102	u	75	165	01110101	117
g	67	147	01100111	103	v	76	166	01110110	118
h	68	150	01101000	104	w	77	167	01110111	119
i	69	151	01101001	105	x	78	170	01111000	120
j	6A	152	01101010	106	y	79	171	01111001	121
k	6B	153	01101011	107	z	7A	172	01111010	122
l	6C	154	01101100	108					
m	6D	155	01101101	109					
n	6E	156	01101110	110					
o	6F	157	01101111	111					
0	30	060	00110000	048	%	25	045	00100101	037
1	31	061	00110001	049	&	26	046	00100110	038
2	32	062	00110010	050	'	27	047	00100111	039
3	33	063	00110011	051	(	28	050	00101000	040
4	34	064	00110100	052	)	29	051	00101001	041
5	35	065	00110101	053	*	2A	052	00101010	042
6	36	066	00110110	054	+	2B	053	00101011	043
7	37	067	00110111	055	,	2C	054	00101100	044
8	38	070	00111000	056	-	2D	055	00101101	045
9	39	071	00111001	057	.	2E	056	00101110	046
SP	20	040	00100000	032	/	2F	057	00101111	047
!	21	041	00100001	033	:	3A	072	00111010	058
"	22	042	00100010	034	;	3B	073	00111011	059
#	23	043	00100011	035	<	3C	074	00111100	060
\$	24	044	00100100	036	=	3D	075	00111101	061
>	3E	076	00111110	062	STX	02	002	00000010	002
?	3F	077	00111111	063	ETX	03	003	00000011	003

CHAR	HEX	OCTAL	BINARY	DEC	CHAR	HEX	OCTAL	BINARY	DEC
@	40	100	01000000	064	EOT	04	004	00000100	004
[	5B	133	01011011	091	ENQ	05	005	00000101	005
\	5C	134	01011100	092	ACK	06	006	00000110	006
]	5D	135	01011101	093	BEL	07	007	00000111	007
^	5E	136	01011110	094	BS	08	010	00001000	008
	5F	137	01011111	095	HT	09	011	00001001	009
{	7B	173	01111011	123	LF	0A	012	00001010	010
	7C	174	01111100	124	VT	0B	013	00001011	011
}	7D	175	01111101	125	FF	0C	014	00001100	012
~	7E	176	01111110	126	CR	0D	015	00001101	013
DEL	7F	177	01111111	127	SO	0E	016	00001110	014
NUL	00	000	00000000	000	SI	0F	017	00001111	015
SOH	01	001	00000001	001	DLE	10	020	00010000	016
D1	11	021	00010001	017					
D2	12	022	00010010	018					
D3	13	023	00010011	019					
D4	14	024	00010100	020					
NAK	15	025	00010101	021					
SYN	16	026	00010110	022					
ETB	17	027	00010111	023					
CAN	18	030	00011000	024					
EM	09	031	00011001	025					
SUB	1A	032	00011010	026					
ESC	1B	033	00011011	027					
FS	1C	034	00011100	028					
GS	1D	035	00011101	029					
RS	1E	036	00011110	030					
US	1F	037	00011111	031					

32 - 126
37 - 126

2^0	1
2^1	2
2^2	4
2^3	8
4	16
5	32
6	64
7	128
8	256
9	512
10	1024
11	2048
12	4096
13	8192
14	16384
15	32768
16	65536

* Base 2 8 bits

- 2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0

- 8 bits = 1 byte

- 16 bits = word

- 32 bits = double word

- 64 bits = sentence

- 4 bits = nibble

* Base 10 Numbers

- $10^5 \ 10^4 \ 10^3 \ 10^2 \ 10^1 \ 10^0$

4562 - $2 \cdot 10^0$, $6 \cdot 10^1$, $5 \cdot 10^2$, $4 \cdot 10^3$

* Base 16 Numbers - Hexadecimal

- 4562 - $2 \cdot 16^0$, $6 \cdot 16^1$, $5 \cdot 16^2$, $4 \cdot 16^3$

* Binary - Base 2

- 0 + 1

- adds to be 255, starts at 0

* B_{10}	B_{16}	B_2
0	0	0000
1	1	0001
2	2	0010
3	3	0011
4	4	0100
5	5	0101
6	6	0110
7	7	0111
8	8	1000
9	9	1001
10	A	1010
11	B	1011
12	C	1100
13	D	1101
14	E	1110
15	F	1111

* Base 8
- 0-7

Base 8	Base 10	Base 16
0000	0	0
1000	1	1
2000	2	2
3000	3	3
4000	4	4
5000	5	5
6000	6	6
7000	7	7
1001	1	1
1010	2	2
1011	3	3
1100	4	4
1101	5	5
1110	6	6
1111	7	7

* * Decimal - Binary

* $1560 \div 2 = 780$

$780 \div 2 = 390$

$390 \div 2 = 195$

$195 / 2 = 97 \text{ r}1$

$97 / 2 = 48 \text{ r}1$

$48 / 2 = 24$

$24 / 2 = 12$

$12 / 2 = 6$

$6 / 2 = 3$

$3 / 2 = 1 \text{ r}1$

$1 / 2 = 0 \text{ r}1$

- 110000011000

* 1560

110000011000

$$\begin{array}{r} 1560 \\ - 1024 \\ \hline 536 \\ 512 \\ \hline 24 \\ 16 \\ \hline 8 \\ 8 \\ \hline 0 \end{array}$$

* $16 \overset{4}{8} \overset{16}{8}$

100000010001000

$$\begin{array}{r} 16384 \\ - 16384 \\ \hline 13864 \\ 128 \\ \hline 0 \\ 0 \\ \hline 0 \end{array}$$

Computer Technology I

Name Brandon Buchanan

Convert the following digits from decimal (base 10) to binary (base 2)

1.) 73

001001

2.) 2053

10000000101

3.) 2824

101100001000

4.) 1046

10000010110

5.) 4170

1000001001010

6.) 12330

11000000101010

7.) 41321

1010000101101001

8.) 37911

1001010001111011

9.) 30900

111100010110100

10.) 65535

1111111111111111

Take the given number and divide by 2, write down remainder and place it furthest to the right. Repeat this process using the remainder until you are left with a zero .
Hint : (you know you are doing it correctly if the answer you get is in the form of all ones or twos)

Example: 1028

$1028/2=514$ $r=0$, $514/2=257$ $r=0$, $257/2=128$ $r=1$, $128/2=64$ $r=0$,
 $64/2=32$ $r=0$, $32/2=16$ $r=0$, $16/2=8$ $r=0$, $8/2=4$ $r=0$, $4/2=2$ $r=0$, $2/2=1$ $r=0$, $1/2=0$ $r=1$

answer: 10000000100

Written by: George Zima

Computer Technology I

Name Brandon Buchanan

Convert the following digits from binary (base 2) to decimal (base 10)

1.) 1010

10

2.) 11000011

195

3.) 00001100

12

4.) 10

2

5.) 00101111

47

6.) 11111111

255

7.) 100000000000

1096

8.) 101010101010

2730

9.) 101100111001101

22989

10.) 1111

15

Place values

MSB ----- LSB

2^{10} 2^9 2^8 2^7 2^6 2^5 2^4 2^3 2^2 2^1 2^0
 1024 512 256 128 64 32 16 8 4 2 1

$$\begin{array}{r} 2560 \\ 14 \\ \hline 2574 \end{array}$$

$$\begin{array}{r} 2048 \\ 256 \\ \hline 2304 \end{array}$$

9096

$$\begin{array}{r} 9096 \\ \times 2 \\ \hline 18192 \end{array}$$

$$\begin{array}{r} 16384 \\ 9096 \\ \hline 25480 \\ + 2509 \\ 196 \\ 13 \\ \hline 23393 \end{array}$$

$$\begin{array}{r} 2048 \\ 256 \\ \hline 2304 \end{array}$$

$$\begin{array}{r} 20480 \\ 2304 \\ 196 \\ 13 \\ \hline 22993 \end{array}$$

$$\begin{array}{r} 16384 \\ 9096 \\ \hline 25480 \end{array}$$

$$\begin{array}{r}
 1. \quad 73 \quad 100/00/ \\
 - 64 \\
 \hline
 9 \\
 8 \\
 + \\
 \hline
 \end{array}$$

$$\begin{array}{r}
 2. \quad 205\frac{1}{2} \quad 1000000000/0/ \\
 - 2048 \\
 \hline
 5 \\
 4 \\
 1 \\
 1 \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 3. \quad 28\frac{1}{2} \quad 10110000/000 \\
 - 2048 \\
 \hline
 776 \\
 512 \\
 264 \\
 256 \\
 \hline
 8 \\
 8 \\
 \hline
 0
 \end{array}$$

$$\begin{array}{r}
 4. \quad 1096 \quad 1000000/001/0 \\
 1028 \\
 \hline
 18 \\
 16 \\
 2 \\
 2 \\
 \hline
 -
 \end{array}$$

$$\begin{array}{r}
 5. \quad 49\frac{1}{2} \quad 1000000/00/010 \\
 9096 \\
 \hline
 79 \\
 64 \\
 10 \\
 8 \\
 2 \\
 2 \\
 \hline
 -
 \end{array}$$

6. $\overset{0}{1}\overset{12}{0}\overset{3}{0}\overset{14}{0}\overset{15}{0}$

11000000101010

$$\begin{array}{r} - 8192 \\ \hline 4188 \\ 9096 \\ \hline 42 \\ 32 \\ \hline 10 \\ 8 \\ \hline 2 \\ 2 \\ \hline - \end{array}$$

7. $\overset{3}{1}\overset{10}{1}\overset{12}{0}\overset{11}{0}\overset{11}{1}$

1010000101101001

$$\begin{array}{r} - 32768 \\ \hline 8883 \\ 8192 \\ \hline 381 \\ 256 \\ \hline 105 \\ 64 \\ \hline 411 \\ 32 \\ \hline 9 \\ 8 \\ \hline 1 \\ 1 \\ \hline 0 \end{array}$$

8. 37911

100101000111011

$- 32768$

$$\begin{array}{r} 514315 \\ \hline 4096 \\ 1147 \\ \hline 1029 \\ 183 \\ \hline 64 \\ 59 \\ 32 \\ \hline 27 \\ 16 \\ \hline 11 \\ 6 \\ \hline 3 \\ 2 \\ \hline 1 \\ 1 \\ \hline - \end{array}$$

9.

30900

11100001010100

16384

9/18/86

8192

6274414

4096

212 213

2098

180

128

5:

3.

2

1

10.

65535

|||||

1. $13 \text{ r } 6$ D6

$$\begin{array}{r} 16 \overline{) 214} \\ \underline{16} \\ 54 \\ \underline{48} \\ 6 \end{array}$$

2. $3E7 \quad 768 + 224 + 7 = 999$

3.

$$\begin{array}{r} 4208 \text{ r } 14 \\ 16 \overline{) 67392} \\ \underline{64} \\ 33 \\ \underline{32} \\ 192 \\ \underline{128} \\ 14 \end{array}$$

$$\begin{array}{r} 263 \text{ r } 0 \\ 16 \overline{) 4208} \\ \underline{32} \\ 100 \\ \underline{96} \\ 48 \end{array}$$

$$\begin{array}{r} 16 \text{ r } 7 \\ 16 \overline{) 263} \\ \underline{16} \\ 103 \\ \underline{96} \\ 7 \end{array}$$

$$\begin{array}{r} 1 \text{ r } 0 \\ 16 \overline{) 16} \\ \underline{16} \\ 0 \end{array}$$

1070E

4.

$$\begin{array}{r} 1297 \text{ r } 1 \\ 16 \overline{) 4753} \\ \underline{32} \\ 155 \\ \underline{144} \\ 113 \\ \underline{112} \\ 1 \end{array}$$

$$\begin{array}{r} 18 \text{ r } 9 \\ 16 \overline{) 297} \\ \underline{16} \\ 137 \\ \underline{128} \\ 9 \end{array}$$

$$\begin{array}{r} 1 \text{ r } 2 \\ 16 \overline{) 18} \\ \underline{16} \\ 2 \end{array}$$

1291

5. $CC00 = (13 \cdot 1096) + (13 \cdot 28) + (0 \cdot 16) + (0 \cdot 1) = 3328$

$$\begin{array}{r} 31 \text{ r } 6 \\ 16 \overline{) 503} \\ \underline{48} \\ 23 \\ \underline{16} \\ 6 \end{array}$$

$$\begin{array}{r} 1 \text{ r } 15 \\ 16 \overline{) 31} \\ \underline{16} \\ 15 \end{array}$$

1F6

$$6. \text{SSAA} = (5 \cdot 9096) + (5 \cdot 256) + (10 \cdot 16) + (10 \cdot 1) = 21152$$

$$7. 2345 = (2 \cdot 9096) + (3 \cdot 256) + (4 \cdot 16) + (5 \cdot 1) = 9029$$

$$8. \text{223ED} = (15 \cdot 65536) + (2 \cdot 9096) + (3 \cdot 256) + (14 \cdot 16) + (13 \cdot 1) = 992037$$

$$9. \begin{array}{r} 5312 \text{ r10} \\ 16 \overline{) 85000} \\ \underline{80} \\ 50 \\ \underline{48} \\ 20 \\ \underline{16} \\ 40 \\ \underline{32} \\ 10 \end{array} \quad \begin{array}{r} 332 \text{ r0} \\ 16 \overline{) 5312} \\ \underline{48} \\ 51 \\ \underline{48} \\ 32 \\ \underline{32} \\ 0 \end{array} \quad \begin{array}{r} 2 \text{ r12} \\ 16 \overline{) 332} \\ \underline{32} \\ 12 \end{array} \quad 2\text{COA}$$

$$10. \begin{array}{r} 81 \text{ r0} \\ 16 \overline{) 1128} \\ \underline{112} \\ 80 \end{array}$$

$$11. 29 = (2 \cdot 16) + (9 \cdot 1) = 41$$

$$12. \begin{array}{r} 66 \text{ r12} \\ 16 \overline{) 1024} \\ \underline{96} \\ 104 \\ \underline{96} \\ 12 \end{array} \quad \begin{array}{r} 4 \text{ r2} \\ 16 \overline{) 66} \\ \underline{64} \\ 2 \end{array} \quad 42($$

Computer Tech I

Combined Numbering Systems

A value is given in one number system. Supply the value for the other two systems.

	Decimal	Hexadecimal
1.	214	06
2.	999	3E7
3.	67342	1070E
4.	4753	1291
5.		CC00
6.	502	1F6
7.	21930	55AA
8.	9029	2345
9.	992257	F23ED
10.	85002	14C0A
11.	128	80
12.	91	29
13.	1024	400
14.	4096	1000
15.	4096	1000
16.	1098576	100000

Hex-Binary-Decimal WS 03

Complete the following table:

Name: Brandon Buchanan

Hex	Bin	Decimal
4E	01001110	78
ED	11101101 128 64 32 16 8 4 2 1	237
FE	11111110	254
37	110111 32 16 8 4 2 1	55
310	110010000	784
AE3	101011100011 128 64 32 16 8 4 2 1	2787
1000	10000000000000	9096
FOO	111100000000 128 64 32 16 8 4 2 1	3840
1001	1000000000001	4097
37F4		14324
3	11	3
12573		75123
2102E	100001000000011110	135214
5CAE		23726

Computer Tech I

Combined Numbering Systems

A value is given in one number system. Supply the value for the other two systems.

	Decimal	Hexadecimal	Binary
1.	214	D6	11010110
2.	999	3E7	1111100111
3.	369	171	101110001
4.	4753	1291	0001001010010001
5.	52224	CC00	1100110000000000
6.	15	F	1111
7.	21930	55AA	0101010110101010
8.	8195	2003	10000000000011
9.	992237	F23ED	1111001000111101101
10.	85002	19C0A	00010100110000001010

$$\begin{array}{r} 11 \\ 256 \\ 369 \\ \hline 1 \end{array}$$

$$\begin{array}{r} 4096 \times 12 = \\ 256 \times 12 = \end{array}$$

$$8192 \times 5 =$$

Pick the Locks

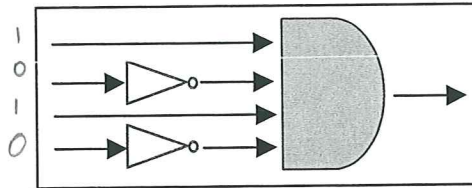
Now the user may test his/her understanding of digital logic by tracing how the input values would pass through the digital logic gates to possibly open the lock.

That is, you should be able to deduce the lock combination by looking at each logic diagram. Once deduced, then test your hypothesis by using those input values.

Note : the cell formulas on this sheet may be unhidden after unprotecting the sheet.

Lock #1

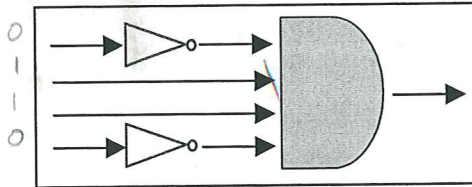
Input A:	1
Input B:	1
Input C:	1
Input D:	1



Output:
0 Locked

Lock #2

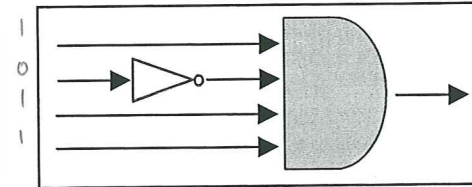
Input A:	1
Input B:	1
Input C:	1
Input D:	1



Output:
0 Locked

Lock #3

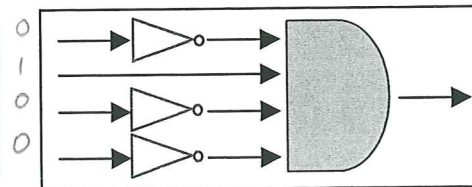
Input A:	1
Input B:	1
Input C:	1
Input D:	1



Output:
0 Locked

Lock #4

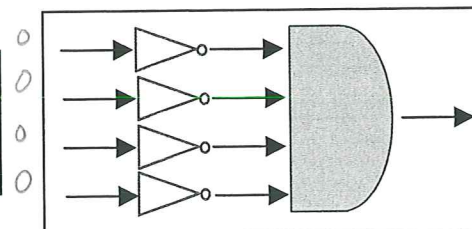
Input A:	1
Input B:	1
Input C:	1
Input D:	1



Output:
0 Locked

Lock #5

Input A:	1
Input B:	1
Input C:	1
Input D:	1



Output:
0 Locked

Question : How many possible combinations are there for a 4-input lock like those above?

Computer Technology

Digital Lock Truth Table

Name

Input Combination				Lock Output				
A	B	C	D	Lock #1	Lock #2	Lock #3	Lock #4	Lock #5
0	0	0	0					
0	0	0	1					
0	0	1	0					
0	0	1	1					
0	1	0	0					
0	1	0	1					
0	1	1	0					
0	1	1	1					
1	0	0	0					
1	0	0	1					
1	0	1	0					
1	0	1	1					
1	1	0	0					
1	1	0	1					
1	1	1	0					
1	1	1	1					

and
xor
or

Logic Gate Intro HW

Perform the operations indicated:

$\overline{1100_2}$ 0011	$11_2 \oplus 10_2$	$11_2 * 10_2$
1. $1001_2 * 1011_2$	$12_{10} + 6_{10}$	$37_{10} + 42_{10}$
$64_h + 53_h$	$\overline{62_h}$	$\overline{1101_2} * D_h$
$23_{10} * 12_h$	$1010_2 + 0011_2 + 1000_2$	$100011_2 * 43_h$
$43_h * 23_h + 52_h$	$43_h + 23_h * 52_h$	$\overline{11000_2} + 11000_2 * 11111_2$
$172_{10} * 192_{10}$	$CD5_h * 4096_{10}$	$10101011001_2 \oplus 123_h$
$CD5_h \oplus 4096_{10}$	$1011010_2 \oplus 0111111_2$	21. $53_{10} * 53_h + 10110_2 \oplus C6_h$

Workspace. Please label.

$$\begin{array}{r}
 21. \quad \begin{array}{r} 00110101 \\ 01010011 \\ \hline 00010001 \end{array} + \begin{array}{r} 00010110 \\ 11000110 \\ \hline 11010000 \end{array} = 11010001 = D1_h
 \end{array}$$

2. $11 \oplus 10 = 01_2$

3. $11 \cdot 10 = 10_2$

4. $1001 \cdot 1011 = 1001$

5. $1100 \cdot 0110 = 0100 = 4$

6. $100101 + 101010 = 101111 = 47_{10}$

7. $01100100 + 01010011 = 01110111 = 77_h$

8. $01100010 = 10011101 = 9D_h$

9. $0010 \cdot 1101 = 0000 = 0_h$

10. $10111 \cdot 10010 = 10010_2 = 12_h$

11. $1011 + 1000 = 1011_2$

12. $0100011 \cdot 1000011 = 0011_2 = 3$

13.

* * Boolean Logic

* Logic Gates

- and or xor

* And

- 

$a, b = \text{inputs}$ $Q = \text{output}$

- $a \cdot b$ (a and b)

- truth tables

a	b	Q
0	0	0
0	1	0
1	0	0
1	1	1

* Or gate (inclusive)

- 

- $a + b$

a	b	Q
0	0	0
0	1	1
1	0	1
1	1	1

* Xor (exclusive)

a	b	Q
0	0	0
0	1	1
1	0	1
1	1	0



$a \oplus b$

* Inverter

- $a \rightarrow \overline{a}$

- $\overline{a}$ is symbol

a	$\overline{a}$
0	1
1	0

* Nor $\Rightarrow \Rightarrow$

- $a + b$

a	b	q
0	0	1
0	1	0
1	0	0
1	1	0

* Nand $\Rightarrow \Rightarrow$

a	b	q
0	0	1
0	1	1
1	0	1
1	1	0

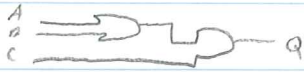
- $a \cdot b$

* Xnor $\Rightarrow \Rightarrow$

a	b	q
0	0	1
0	1	0
1	0	0
1	1	1

$a \oplus b$

X



$$(A + B) \cdot C$$

A	B	C	Q		
0	0	0	0	0	0
0	0	1	0	1	0
0	1	0	0	2	0
0	1	1	1	3	1
1	0	0	0	4	0
1	0	1	1	5	1
1	1	0	0	6	0
1	1	1	1	7	1

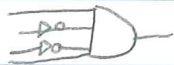
1.

* negative OR



a	b	O
0	0	0
0	1	1
1	0	0
1	1	0

*

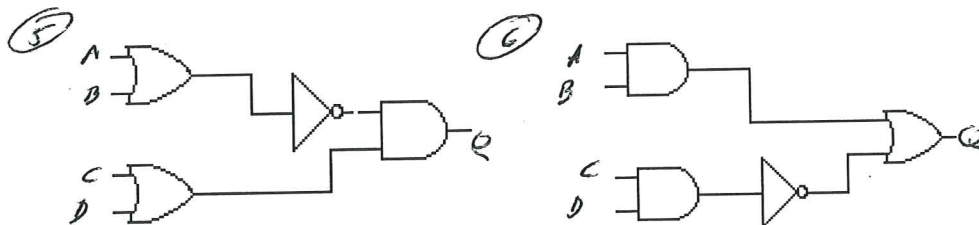
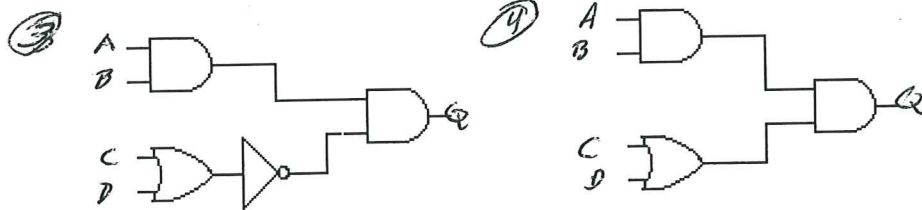
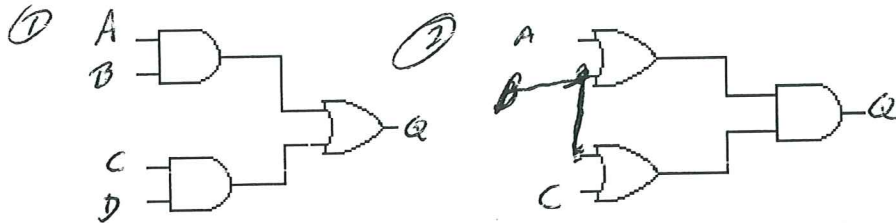


$$Q = 1$$

9.10.09

Simple Combo TT

For each of the following, complete a truth table



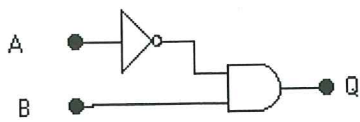
(1)

A	B	C	D	Q

5.

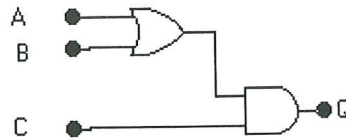
A	B	C	D	Q
0	0	0	0	0
0	0	0	1	1
0	0	1	0	1
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$$(\overline{A} + B) \cdot (C + \overline{D})$$

Boolean Exp $\bar{A} \cdot \bar{B}$

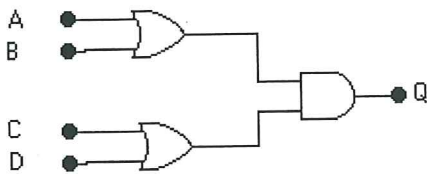
Truth Table

A	B	Q
0	0	0
0	1	1
1	0	0
1	1	0

Boolean Exp $(A+B) \cdot C$

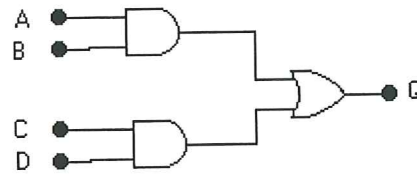
Truth Table

A	B	C	Q
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	0
1	1	1	1

Boolean Exp $(A+B) \cdot (C+D)$

Truth Table

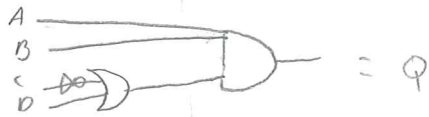
A	B	C	D	Q
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	1
0	1	1	0	1
0	1	1	1	1
1	0	0	0	0
1	0	0	1	1
1	0	1	0	1
1	0	1	1	1
1	1	0	0	0
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

Boolean Exp $(A \cdot B) + (C \cdot D)$

Truth Table

A	B	C	D	Q
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

$$A \cdot B \cdot (\bar{C} + D) = Q$$



$$\overline{A} B C$$

Show all work in space provided- no work, no credit

93

1) $1101_b = \underline{13}_h$ <i>Handwritten: 13</i>	2) $101101_b = \underline{45}_{10}$ <i>Handwritten: 10+9+1</i>	3) $124_{10} = \underline{0111100}_b$ <i>Handwritten: 16 124 = 7 r 12, 07 12h = 0111 1100b</i>
4) $2E4_h = \underline{001011100100}_b$ <i>Handwritten: 0010 1110 0100, 2 E 4</i>	5) $135_{10} = \underline{87}_h$ <i>Handwritten: 10000111, 128 + 4 + 16 + 8 + 4 + 2 + 1 = 135, 1000 0111, 8 7</i>	6) $EF_h = \underline{239}_{10}$ <i>Handwritten: 15 * 1 = 15, 14 * 16 = 224, 239</i>
7) $11101100_b = \underline{EC}_h$ <i>Handwritten: E C</i>	8) $254_h = \underline{596}_{10}$ <i>Handwritten: 10 0101 0100, 512 + 64 > 576, 16 > 20, 596</i>	9) $1259_{10} = \underline{10011101001}_b$ <i>Handwritten: 16 1259 = 78 r 11, 4 14 11h, 0100 1110 1001, 1011</i>

$$10) 65537_{10} = 10001_h$$

$$\begin{array}{r} 4096 \text{ r } 1 \\ 16 \overline{) 65537} \\ \underline{64} \\ 153 \\ \underline{144} \\ 97 \\ \underline{96} \\ 1 \\ 256 \text{ r } 0 \\ 16 \overline{) 4096} \\ \underline{32} \\ 89 \\ \underline{80} \\ 96 \\ \underline{96} \\ 0 \end{array}$$

$$11) 45A2_h = 17826_{10}$$

$$\begin{array}{r} 2 \cdot 1 = 2 \\ 10 \cdot 16 = 160 > 162 \\ 5 \cdot 256 = 1280 \\ 4 \cdot 9096 = 36384 \\ \hline 17826 \end{array}$$

$$12) 9000_{10} = 0010 \ 0011 \ 0010 \ 1000_b$$

$$\begin{array}{r} 560 \text{ r } 8 \\ 16 \overline{) 9000} \\ \underline{80} \\ 100 \\ \underline{96} \\ 40 \\ \underline{32} \\ 8 \\ \underline{8} \\ 0 \\ 35 \text{ r } 2 \\ 16 \overline{) 560} \\ \underline{48} \\ 80 \\ \underline{80} \\ 0 \end{array}$$

$$13) 333_h = 0011 \ 0011 \ 0011_b$$

$$\begin{array}{r} 0011 \ 0011 \ 0011 \\ 3 \ 3 \ 3_h \end{array}$$

$$14) 110011001100_b = 3276_{10}$$

$$\begin{array}{r} 12 \cdot 1 = 12 \\ 12 \cdot 16 = 192 > 204 \\ 12 \cdot 256 = 3072 \\ \hline 3276 \end{array}$$

$$15) 8192_{10} = 10 \ 0000 \ 0000 \ 0000_b$$

$$\begin{array}{r} 512 \text{ r } 0 \\ 16 \overline{) 8192} \\ \underline{80} \\ 19 \\ \underline{16} \\ 32 \\ \underline{32} \\ 0 \\ 32 \text{ r } 0 \\ 16 \overline{) 512} \\ \underline{48} \\ 32 \\ \underline{32} \\ 0 \\ 32 \text{ r } 0 \\ 16 \overline{) 32} \\ \underline{32} \\ 0 \end{array}$$

$$16) 145237_{10} = 23755_h$$

$$\begin{array}{r} 9077 \text{ r } 5 \\ 16 \overline{) 145237} \\ \underline{128} \\ 172 \\ \underline{160} \\ 117 \\ \underline{112} \\ 57 \\ 567 \text{ r } 5 \\ 16 \overline{) 9077} \\ \underline{80} \\ 107 \\ \underline{96} \\ 117 \\ \underline{112} \\ 5 \end{array}$$

$$17) 45EE3_h = 286435_{10}$$

$$\begin{array}{r} 3 \cdot 1 = 3 \\ 17 \cdot 16 = 272 \\ 17 \cdot 256 = 4352 \\ 5 \cdot 9096 = 45480 \\ 4 \cdot 65536 = 262144 \\ \hline 286435 \end{array}$$

$$18) 511_{10} = 1 \ 1111 \ 1111_b$$

$$\begin{array}{r} 31 \text{ r } 15 \\ 16 \overline{) 511} \\ \underline{48} \\ 31 \\ \underline{32} \\ 15 \\ 1 \text{ r } 15 \\ 16 \overline{) 31} \\ \underline{16} \\ 15 \end{array}$$

$$19) 1048576_{10} = 100000_h$$

$$\begin{array}{r} 65536 \text{ r } 0 \\ 16 \overline{) 1048576} \\ \underline{96} \\ 88 \\ \underline{80} \\ 85 \\ \underline{80} \\ 57 \\ 98 \\ \underline{96} \\ 2 \end{array}$$

$$20) 196608_{10} = 0011 \ 0000 \ 0001 \ 0100 \ 0000_b$$

$$\begin{array}{r} 12288 \text{ r } 0 \\ 16 \overline{) 196608} \\ \underline{16} \\ 36 \\ \underline{32} \\ 46 \\ \underline{32} \\ 140 \\ \underline{128} \\ 128 \\ \underline{128} \\ 0 \end{array}$$

1. $(A \cdot B) + (C \cdot D)$

A	B	C	D	Q
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	1
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	1
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	1
1	1	0	0	1
1	1	0	1	1
1	1	1	0	1
1	1	1	1	1

2. $(A + B) \cdot (B + C)$

A	B	C	Q
0	0	0	0
0	0	1	0
0	1	0	1
0	1	1	1
1	0	0	0
1	0	1	1
1	1	0	1
1	1	1	1

3.

A	B	C	D	Q
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	1
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0

$$(A \cdot B) \cdot (\overline{C} + D)$$

4.

A	B	C	D	Q
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	1
1	1	1	1	1

$$(A \cdot B) \cdot (C + D)$$

4-20

a

$$BD + B(D+E) + \bar{D}(D+F)$$

$$BD + BD + BE + \bar{D}D + \bar{D}F$$

$$BD + BE + \bar{D}F$$

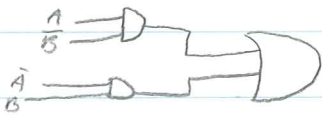
b

$$\bar{A}\bar{B}C + (\overline{A+B+C}) + \bar{A}\bar{B}\bar{C}\bar{D}$$

Brandon Buchanan

4-17

a



b

PROBLEMS

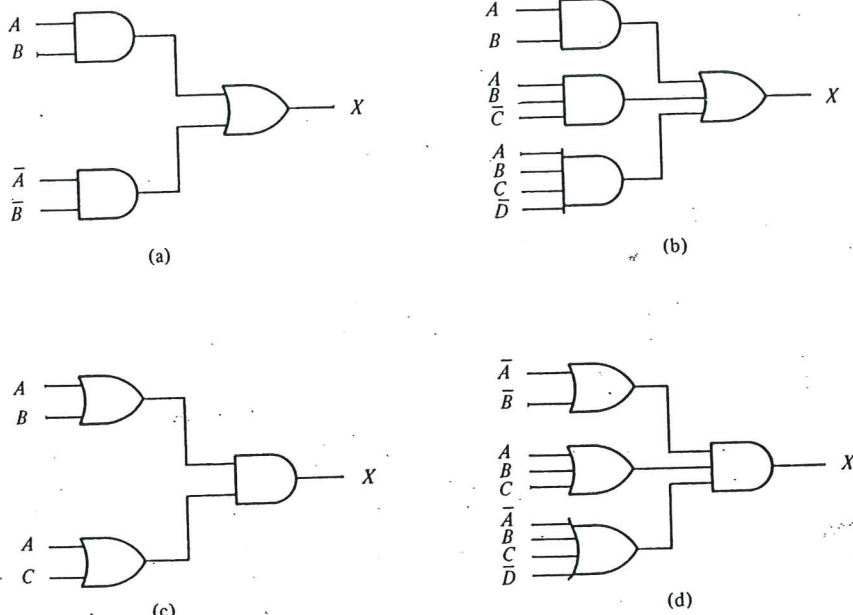


FIGURE 4-34

4-16 Draw the logic circuit represented by each of the following expressions:

- (a) $A + B + C$ (b) $\overline{ABC}$ (c) $AB + C$
 (d) $AB + CD$ (e) $\overline{AB}(C + \overline{D})$

4-17 Draw the logic circuit represented by each expression.

- (a) $A\overline{B} + \overline{A}B$ (b) $AB + \overline{A}\overline{B} + \overline{A}BC$ (c) $A + B[C + D(B + \overline{C})]$

Section 4-6

4-18 Simplify as much as possible the following expressions, using Boolean algebra techniques:

- (a) $A(A + B)$ (b) $A(\overline{A} + AB)$ (c) $BC + \overline{B}C$
 (d) $A(A + \overline{A}B)$ (e) $\overline{A}\overline{B}C + \overline{A}BC + \overline{A}\overline{B}C$

4-19 Simplify the following expressions, using Boolean algebra:

- (a) $(A + \overline{B})(A + C)$ (b) $\overline{A}B + \overline{A}B\overline{C} + \overline{A}BCD + \overline{A}B\overline{C}DE$
 (c) $AB + \overline{A}\overline{B}C + A$ (d) $(A + \overline{A})(AB + \overline{A}B)$
 (e) $AB + (\overline{A} + \overline{B})C + AB$

4-20 Simplify each expression, using Boolean algebra:

- (a) $\overline{B}D + B(D + E) + \overline{D}(D + F)$
 (b) $\overline{A}\overline{B}C + (A + B + \overline{C}) + \overline{A}\overline{B}CD$
 (c) $(B + BC)(B + \overline{B}C)(B + D)$
 (d) $ABCD + AB(\overline{C}\overline{D}) + (\overline{A}B)CD$
 (e) $ABC[AB + \overline{C}(BC + AC)]$

4-23

a

	$\bar{A}\bar{B}$	$\bar{A}B$	AB	$A\bar{B}$
$\bar{C}$	1			
C	1	1		

$\bar{A}\bar{B} + \bar{B}C$

b $\bar{A}\bar{B}C + AC$

	$\bar{A}\bar{C}$	$\bar{A}C$	AC	$A\bar{C}$
$\bar{B}$			1	
B				

$AC + \bar{B}$

c $\bar{A}BC + \bar{A}B\bar{C} + ABC + AB\bar{C}$

$\bar{A}BC + \bar{C} + ABC + \bar{C}$

$ABC + \bar{C} + ABC \quad BC + A + \bar{C}$

	$\bar{A}\bar{B}$	$\bar{A}B$	AB	$A\bar{B}$
$\bar{C}$		1	1	
C		1	1	

AB

d $\bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C}$

	$\bar{A}\bar{B}$	$\bar{A}B$	AB	$A\bar{B}$
$\bar{C}$	1	1	1	1
C				

e $A + \bar{B}C$

	$\bar{B}\bar{C}$	$B\bar{C}$	BC	$\bar{B}C$
A				1
$\bar{A}$				

7-24

Section 4-7

- 4-21 What size Karnaugh map (number of cells) is required if the number of variables in an expression is
 (a) 2 (b) 3 (c) 4 (d) 5
- 4-22 Using the Karnaugh map method, simplify the following expressions to their minimum sum-of-products form:
 (a) $X = \overline{A}\overline{B} + A\overline{B}$ (b) $X = \overline{A}\overline{B} + \overline{A}B$
 (c) $X = \overline{A}\overline{B} + AB$ (d) $X = \overline{A}\overline{B} + \overline{A}\overline{B} + \overline{A}B + AB$
 (e) $X = A(\overline{B} + AB)$ (f) $X = \overline{A}\overline{B} + AB$
- 4-23 Use a Karnaugh map to find the minimum sum-of-products form for each expression.
 (a) $X = \overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + A\overline{B}C$
 (b) $X = AC(\overline{B} + C)$
 (c) $X = \overline{A}(BC + \overline{B}\overline{C}) + A(BC + \overline{B}\overline{C})$
 (d) $X = \overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + \overline{A}B\overline{C} + A\overline{B}\overline{C}$
 (e) $X = A + \overline{B}C$
- 4-24 Use a Karnaugh map to simplify each function to a minimum sum-of-products form.
 (a) $X = \overline{A}\overline{B}\overline{C} + \overline{A}\overline{B}C + \overline{A}BC + A\overline{B}\overline{C}$
 (b) $X = AC[\overline{B} + A(B + \overline{C})]$
 (c) $X = DE\overline{F} + \overline{D}E\overline{F} + \overline{D}E\overline{F}$
- 4-25 Use a Karnaugh map to reduce each expression to a minimum sum-of-products.
 (a) $X = A + \overline{B}\overline{C} + CD$
 (b) $X = \overline{A}\overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}C\overline{D} + ABCD + A\overline{B}C\overline{D}$
 (c) $X = \overline{A}B(\overline{C}\overline{D} + \overline{C}D) + AB(\overline{C}\overline{D} + \overline{C}D) + A\overline{B}\overline{C}\overline{D}$
 (d) $X = (\overline{A}\overline{B} + \overline{A}B)(CD + \overline{C}\overline{D})$
 (e) $X = \overline{A}\overline{B} + \overline{A}B + \overline{C}\overline{D} + C\overline{D}$
- 4-26 Repeat Problem 4-25 for the following expressions:
 (a) $X = \overline{A}(\overline{B}\overline{C}\overline{D} + \overline{B}C\overline{D}) + A(\overline{B}\overline{C}\overline{D} + \overline{B}C\overline{D})$
 (b) $X = B[\overline{A}\overline{C}\overline{D} + \overline{A}C\overline{D}] + (A\overline{C}\overline{D} + A\overline{C}\overline{D})$
 (c) $X = \overline{A}\overline{B} + \overline{A}B + \overline{A}\overline{B}\overline{C}\overline{D} + \overline{A}\overline{B}C\overline{D}$

7-25

a

	$\bar{A}\bar{B}$	$\bar{A}B$	AB	$A\bar{B}$
$\bar{C}\bar{D}$			1	1
$\bar{C}D$			1	1
$C\bar{D}$	1	1	1	1
CD		1	1	1

b

$$\bar{A}\bar{B}\bar{C}\bar{D} + \bar{A}\bar{B}\bar{C}D + A\bar{B}C\bar{D} + A\bar{B}CD$$

$$\bar{C}\bar{D} + \bar{C}D + C\bar{D} + CD$$

	$\bar{A}\bar{B}$	$\bar{A}B$	AB	$A\bar{B}$
$\bar{C}\bar{D}$	1			
$\bar{C}D$	1			
$C\bar{D}$			1	
CD			1	

d

$$(\bar{A}\bar{B} + A\bar{B})(\bar{C}D + C\bar{D})$$

$$(\bar{A}B)(C)$$

$$\bar{A}C$$

	$\bar{A}\bar{B}$	$\bar{A}B$	AB	$A\bar{B}$
$\bar{C}\bar{D}$	1	1		
$\bar{C}D$	1	1	1	1
$C\bar{D}$	1	1	1	1
CD	1	1		

$$\bar{B} + BC$$

Boolean Laws

1. Commutative Law $A+B = B+A$ $AB=BA$
2. Associative Law $A+(B+C) = (A+B)+C$ $A(BC) = (AB)C$
3. Distributive Law $A(B+C) = AB+AC$

4. Rules

1. $A+0=A$
2. $A+1=1$
3. $A*0=0$
4. $A*1=A$
5. $A+A=A$
6. $A+\bar{A}=1$
7. $A*A=A$
8. $A*\bar{A}=0$
9. $\bar{\bar{A}}=A$
10. $A+AB=A$
11. $A+\bar{A}B=A+B$
12. $(A+B)(A+C)=A+BC$

5. DeMorgans Theorem

$$\overline{AB} = \bar{A} + \bar{B}$$

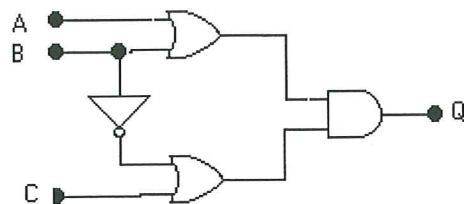
$$\overline{A+B} = \bar{A}\bar{B}$$

$$A \oplus B = \bar{A}B + A\bar{B}$$

$$\overline{A \oplus B} = \overline{\bar{A}B + A\bar{B}} = \bar{\bar{A}B} \bar{A\bar{B}} = \bar{\bar{A}}\bar{B} \bar{A}\bar{\bar{B}} = AB + \bar{A}\bar{B}$$

Review for Quiz on logic gates

- 1) Write the non-minimized Boolean Exp for this circuit. $(A+B) \cdot (\bar{B}+C)$



$$(A+B) \cdot (\bar{B}+C)$$

- 2) $1001_2 * 1011_2 = 1001_2$

- 3) Using Boolean Alg, reduce this to minimal form

$$Q = AB + \bar{A}\bar{B} + A\bar{B}$$

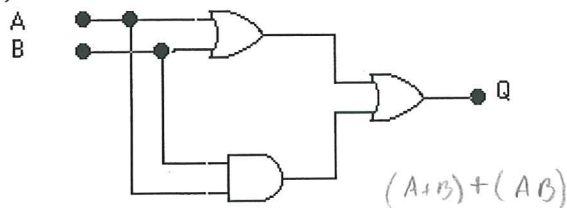
$$AB + \bar{A}\bar{B} + A\bar{B} = AB + \bar{B}(\bar{A} + A) = AB + \bar{B}$$

- 4) Create the minimized circuit that will generate the following truth table.

A	B	C	Q
0	0	0	0
0	0	1	1
0	1	0	1
0	1	1	0
1	0	0	1
1	0	1	1
1	1	0	0
1	1	1	1

	$\bar{A}\bar{B}$	$\bar{A}B$	$A\bar{B}$	AB
$\bar{C}$	0	1	1	0
C	1	1	1	1

- 5) Write the truth table for the circuit shown.



A	B	Q
0	0	0
0	1	0
1	0	0
1	1	1

- 6) Using Karnaugh mapping, find and Draw minimized circuit.

$$Q = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + A\bar{B}\bar{C} = \bar{C}$$



- 7) $CD5_h \oplus 4096_{10} = 1000_h$

- 8) Draw the minimal circuit

$$Q = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + A\bar{B}\bar{C}$$

$$\bar{A}\bar{B}(\bar{C}+C)$$

$$\bar{A}\bar{B} + A\bar{B}\bar{C}$$

$$\bar{B}(\bar{A} + A\bar{C})$$